



An Introduction to Mass Spectrometry and
Applications to Trace and Ultra-Trace
Analysis

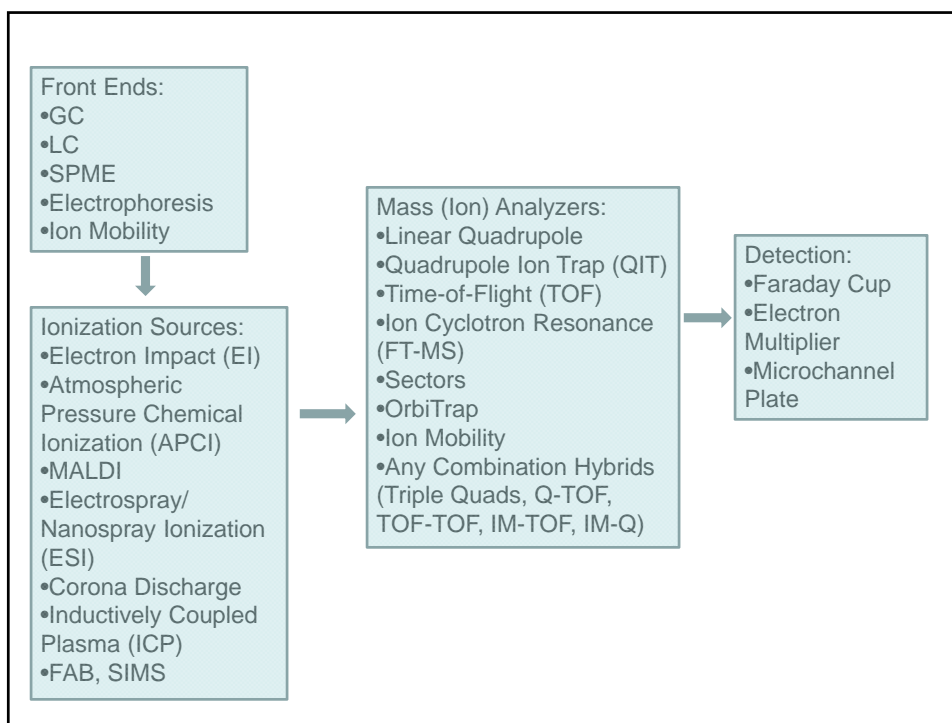
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University of North Texas
Director: UNT-Laboratory for Imaging Mass Spectrometry

What is Trace? Ultra-Trace?

Trace:
ppt (thousand)
-ppm

	1	0.001	0.000001	0.000000001	Grams in 1L (1000g)
amu	1ppt	1ppm	1ppb	1ppt	
10	1.00E-01	1.00E-04	1.00E-07	1.00E-10	
100	1.00E-02	1.00E-05	1.00E-08	1.00E-11	
1000	1.00E-03	1.00E-06	1.00E-09	1.00E-12	
10000	1.00E-04	1.00E-07	1.00E-10	1.00E-13	molar

Ultra Trace:
<ppb



Sensitivity vs Selectivity:

$$\text{Sensitivity} = \frac{\# \text{ of } - \text{ species } - \text{ detected}}{\text{total } - \# \text{ of } - \text{ species}}$$

$$1 - \text{Selectivity} = \frac{\# \text{ of } - \text{ false } - \text{ positives } - \text{ detected}}{\text{total } - \# \text{ of } - \text{ false } - \text{ positives}}$$

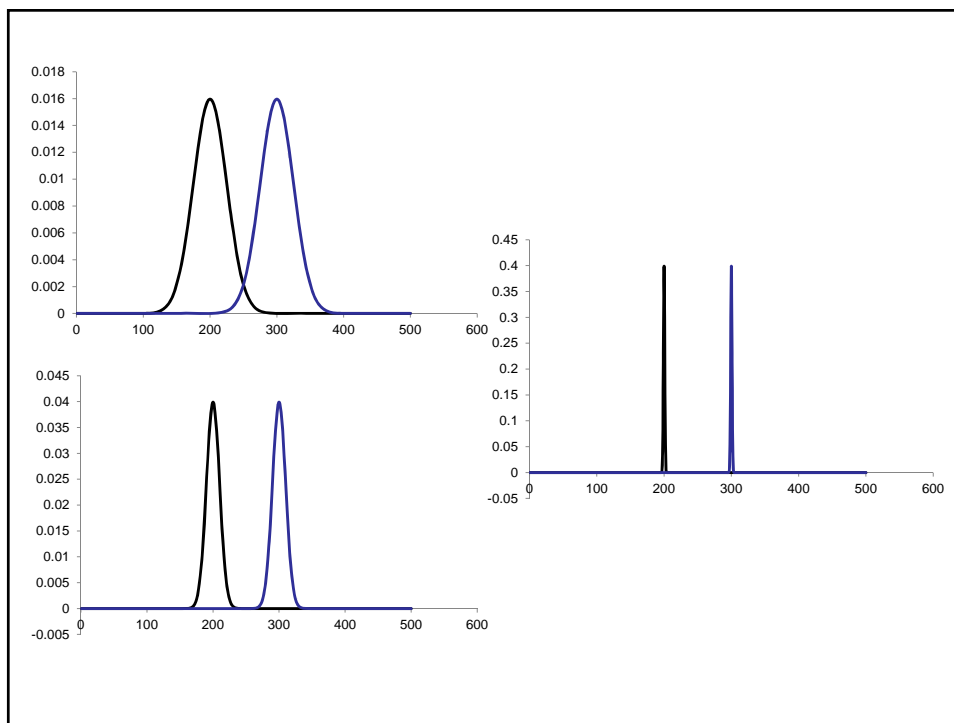
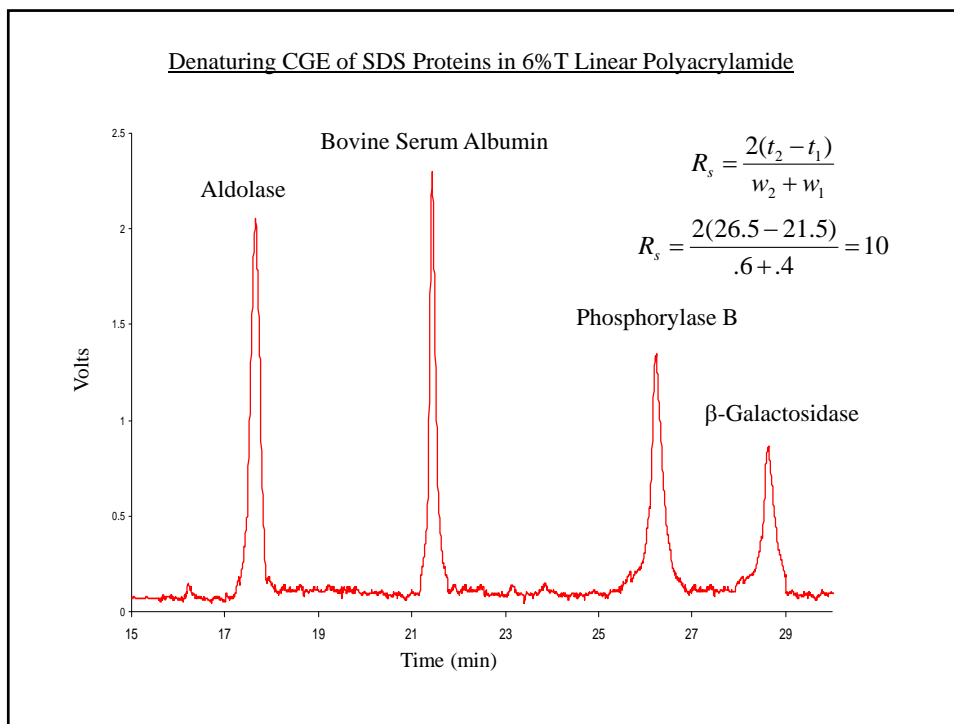
Resolution vs Resolving Power (MS):

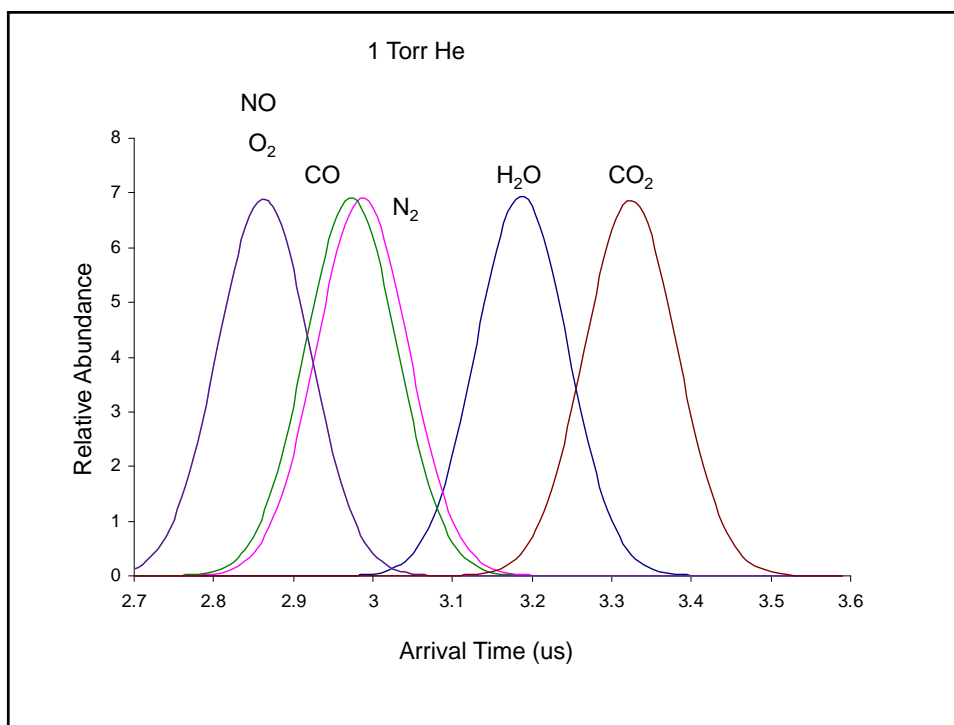
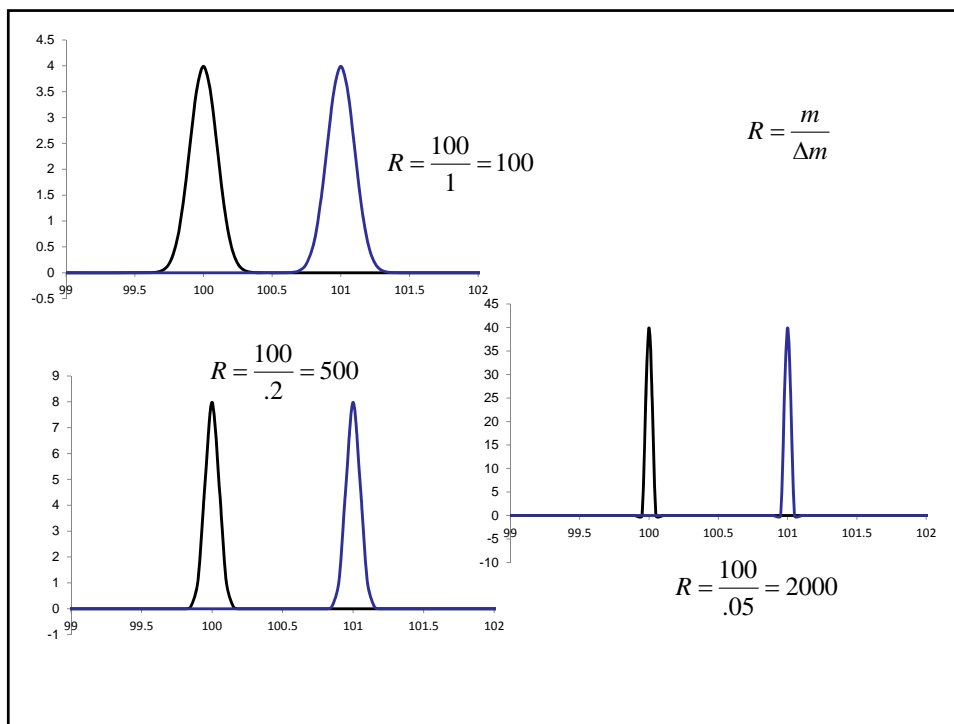
$$\text{Resolution} = \frac{m}{\Delta m}$$

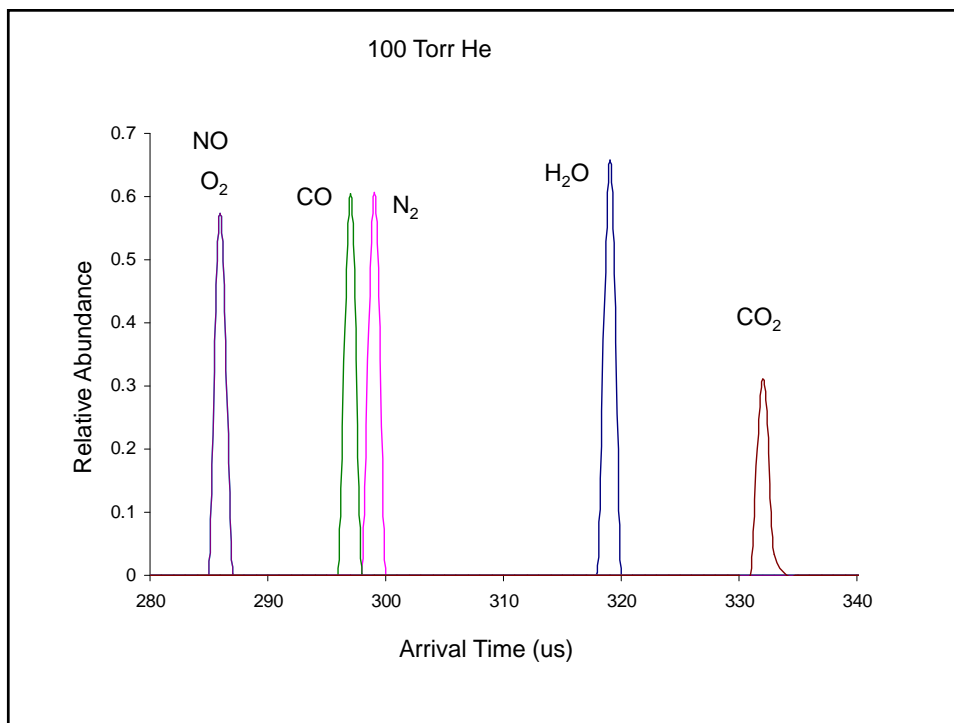
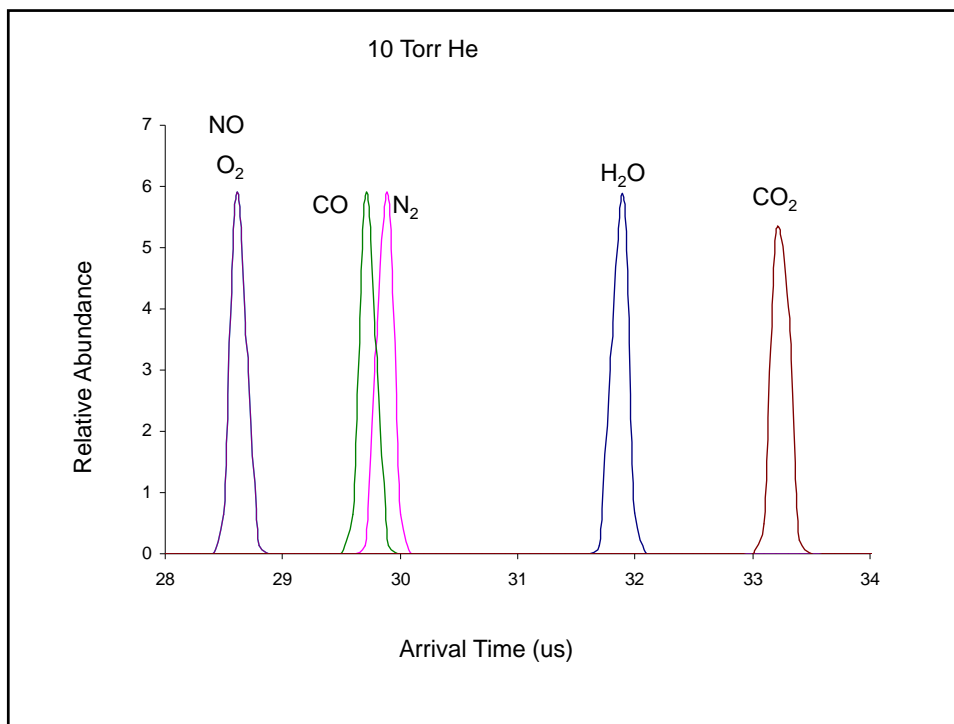
$$\text{Resolving Power} = \Delta m$$

Resolution Chromatography:

$$R_s = \frac{2(t_2 - t_1)}{w_2 + w_1}$$





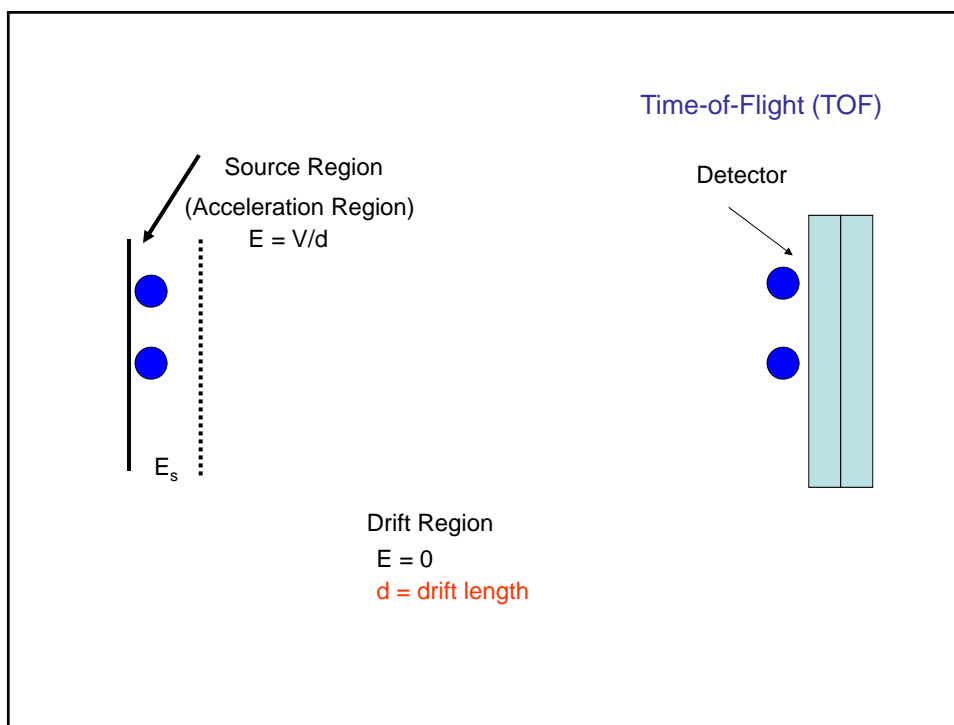
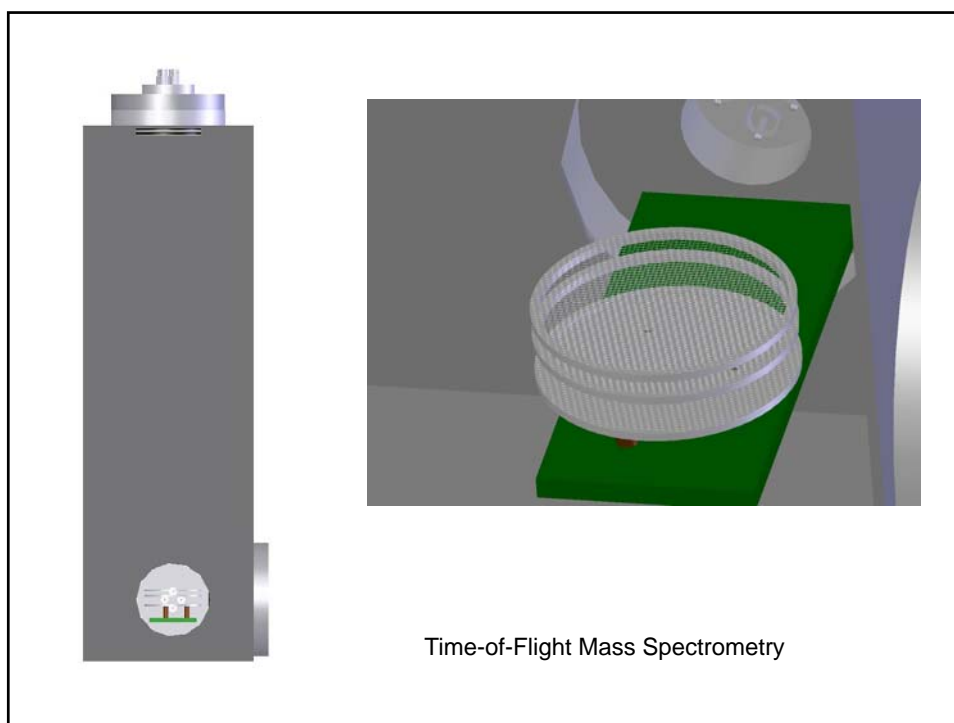


Why is resolution so important?

Z	Name	Symbol	Mass of Atom (u)	% Abundance
1	Hydrogen	^1H	1.007825	99.9885
	Deuterium	^2H	2.014102	0.115
	Tritium	^3H	3.016049	*
6	Carbon	^{12}C	12.000000	98.93
		^{13}C	13.003355	1.07
		^{14}C	14.003242	*
7	Nitrogen	^{14}N	14.003074	99.632
		^{15}N	15.000109	0.368
8	Oxygen	^{16}O	15.994915	99.757
		^{17}O	16.999132	0.038
		^{18}O	17.999160	0.205

Mass Analyzers:





Time-of-Flight (TOF)

$$eV = \frac{1}{2}mv^2 \quad \text{Kinetic Energy given to the Ion in the Source Region}$$

$$v = \left(\frac{2eV}{m} \right)^{\frac{1}{2}} \quad \text{Solving for Velocity}$$

$$v = \frac{d}{t} \quad \text{Solve for Flight Time} \quad t = \left(\frac{m}{2eV} \right)^{\frac{1}{2}} d$$

So, with a constant acceleration voltage and a known drift length, the drift time is proportional to the square root of the mass to charge ratio (m/e).

Time-of-Flight (TOF)

Mass spectrometrists define resolution as: $\frac{m}{\Delta m}$

In TOF we start from the drift time equation:

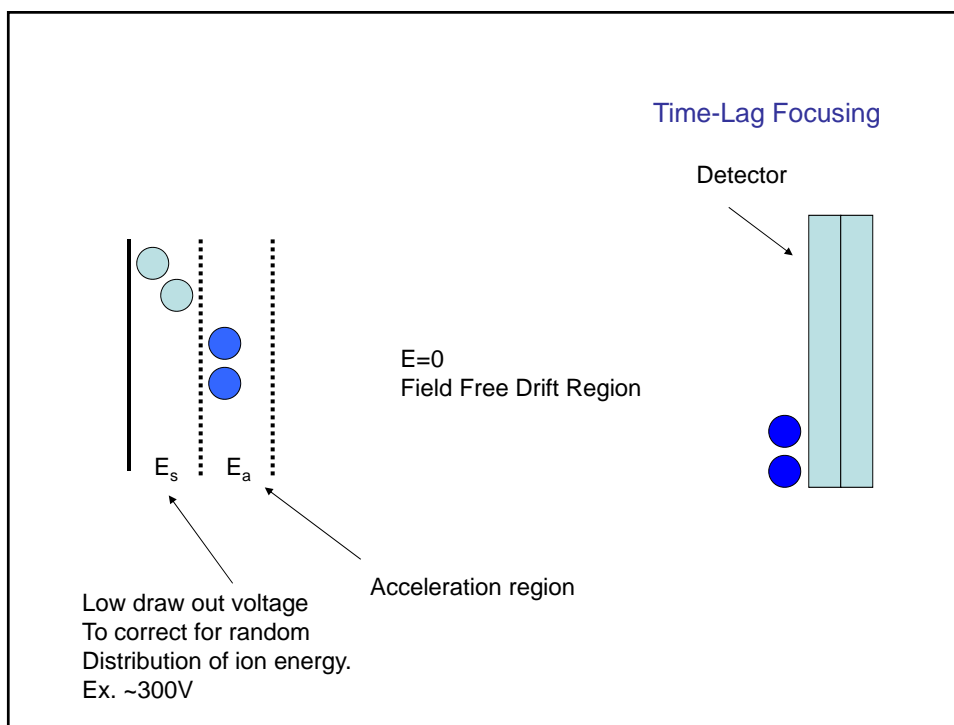
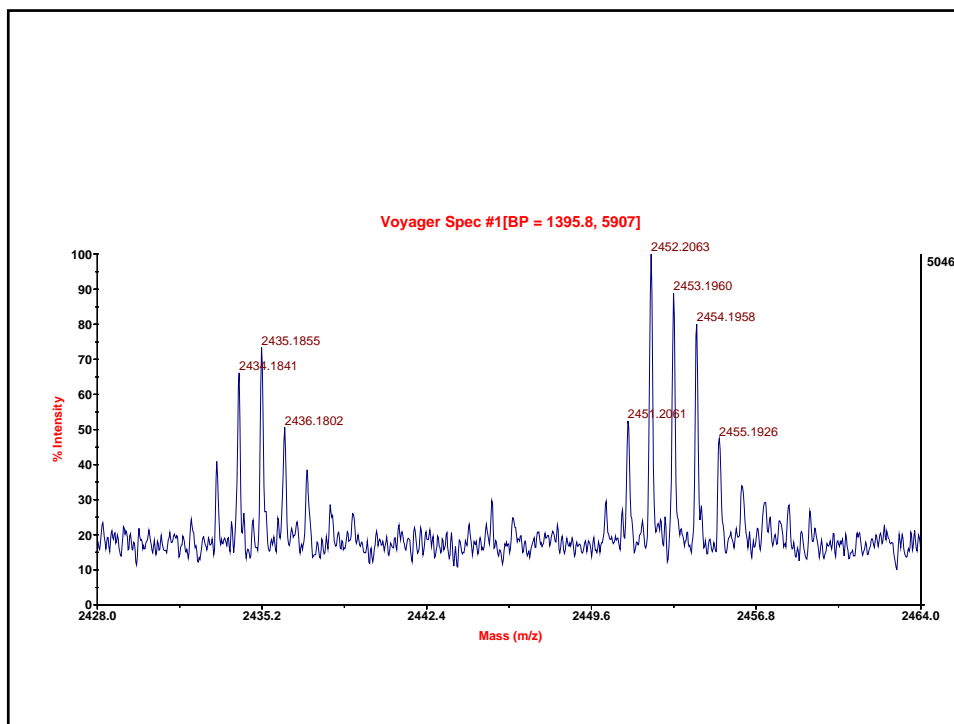
$$m = \left(\frac{2eV}{d^2} \right) t^2 \quad \text{And the derivative is:} \quad dm = \left(\frac{2eV}{d^2} \right) 2t dt$$

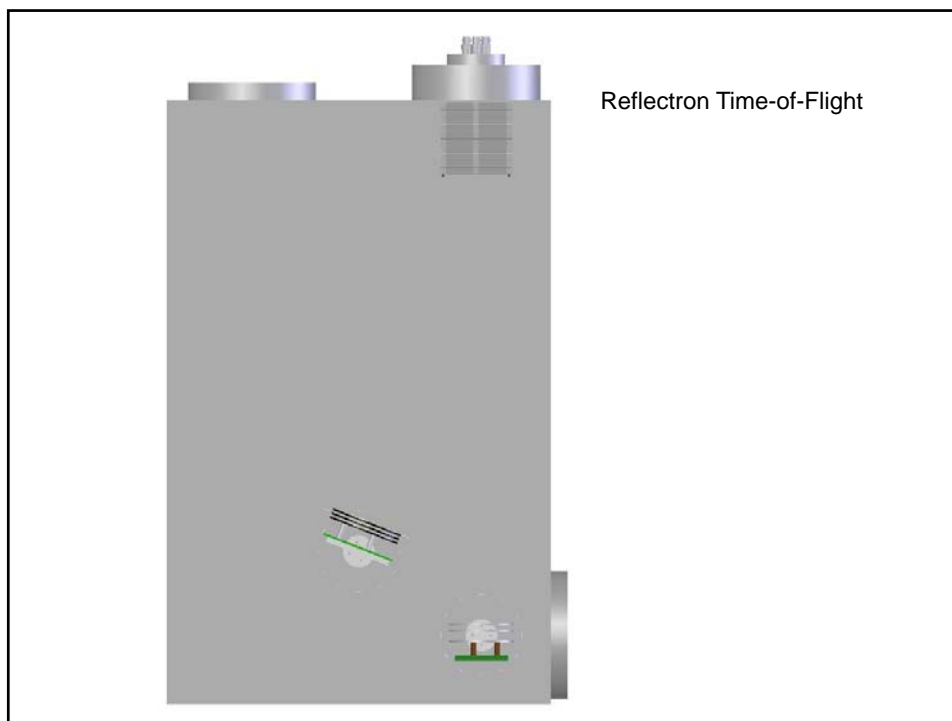
So,

So time-of-flight resolution is defined by:

$$\frac{m}{dm} = \frac{t}{2dt} \quad R = \frac{m}{\Delta m} = \frac{t}{2\Delta t} \quad R \propto \frac{L}{E_z}$$

Δt is usually defined a peak width at half height.





Quadrupole Mass Spectrometry

The Quadrupole Field

The potential at any point (x,y,z) is defined as:

$$\phi = \frac{\phi_o}{r_o^2} (\lambda x^2 + \sigma y^2 + \gamma z^2)$$

Where,

ϕ_o = the applied field

λ, σ, γ are weighing constants for their coordinate

r_o = constant for the device

The applied field is the combination of a RF and DC (U) field:

$$\phi_o = U - V \cos(\Omega t)$$

V = 0 to Peak

Ω (rad/s) = $2\pi f$ (Hz)

Linear Quads

$$\phi = \frac{\phi_o}{r_o^2} (\lambda x^2 + \sigma y^2 + \gamma z^2)$$

We remember the constraints from the Laplace eq.:

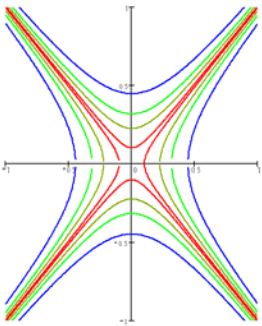
$$\lambda + \sigma + \gamma = 0$$

If we are only interested in quadrupole MS (x,y) then:

$$\gamma = 0$$

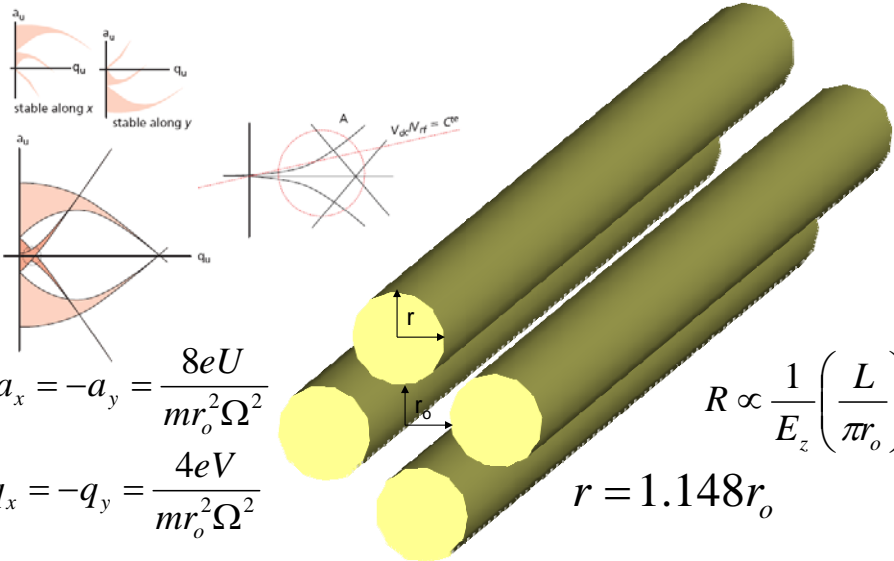
$$\lambda = -\sigma$$

If we set $\lambda=1$, then:

$$\phi = \frac{\phi_o}{r_o^2} (x^2 - y^2)$$


The equipotential field plot

Linear Quads



$$a_x = -a_y = \frac{8eU}{mr_o^2 \Omega^2}$$

$$q_x = -q_y = \frac{4eV}{mr_o^2 \Omega^2}$$

$$R \propto \frac{1}{E_z} \left(\frac{L}{\pi r_o} \right)^2$$

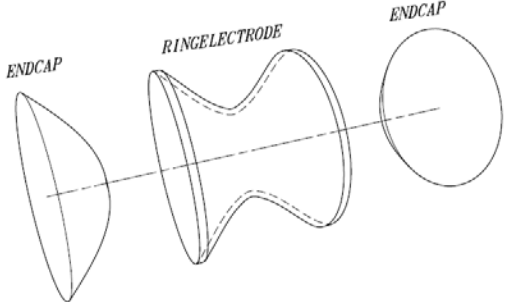
$$r = 1.148 r_o$$

Quad Ion Traps

$$\lambda + \sigma + \gamma = 0$$

$$\lambda = \sigma = 1$$

$$\gamma = -2$$

$$\phi = \frac{\phi_o}{r_o^2} (x^2 + y^2 - 2z^2)$$


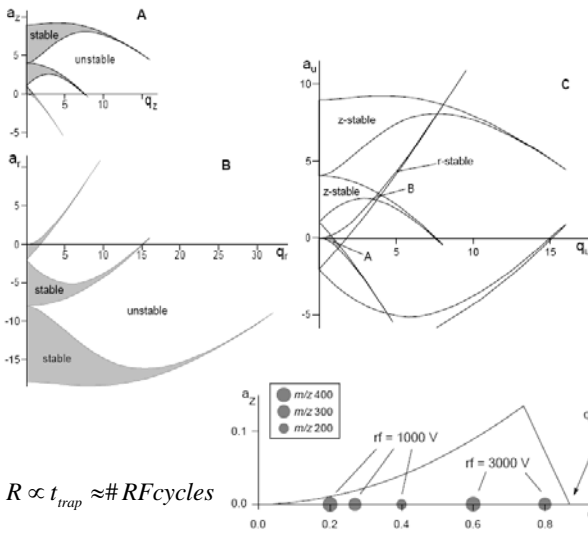
Transform into cylindrical coordinates:

$$\phi = \frac{\phi_o}{r_o^2} (r^2 \cos^2 \theta + r^2 \sin^2 \theta - 2z^2) \quad (\cos^2 \theta + \sin^2 \theta = 1)$$

$$\phi = \frac{\phi_o}{r_o^2} (r^2 - 2z^2)$$

Geometrical constraints:
 $r_o^2 = 2z_o^2$

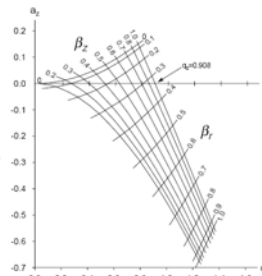
Quad Ion Traps

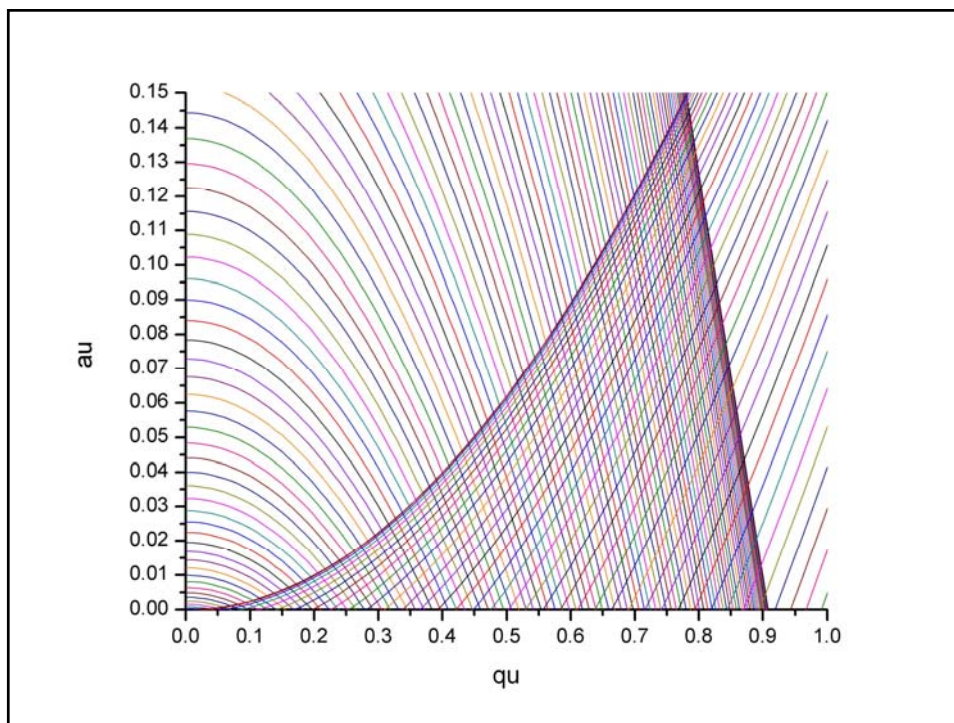
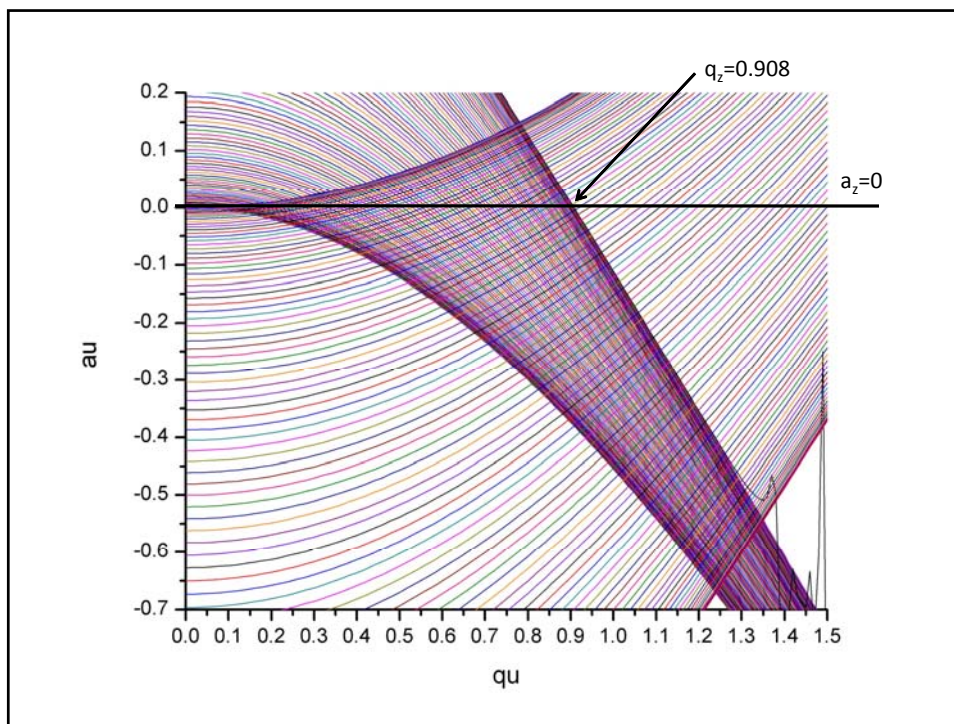


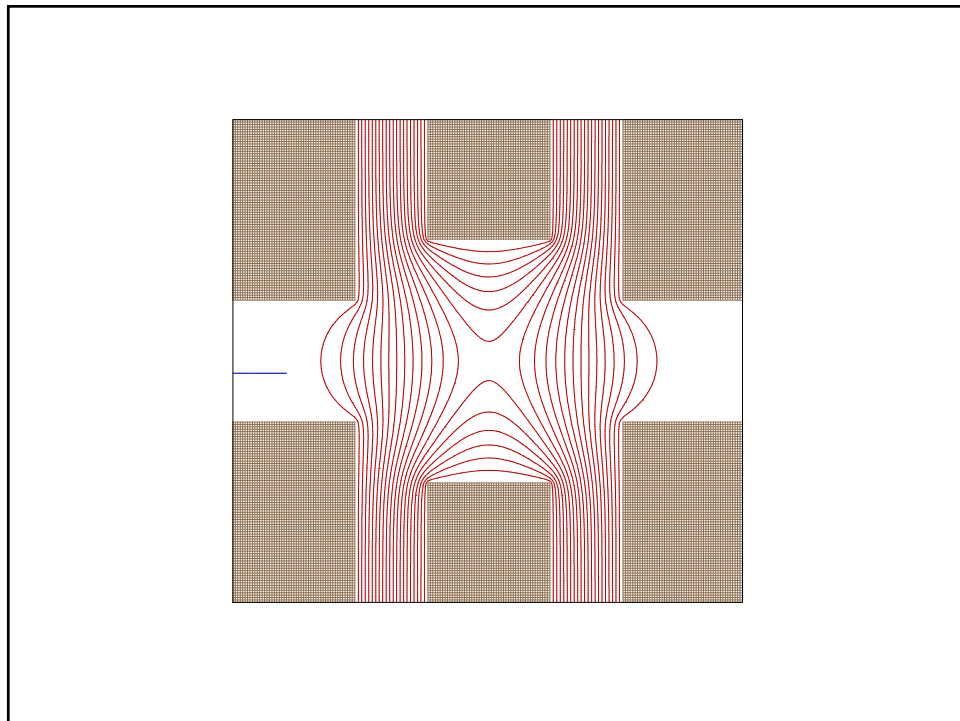
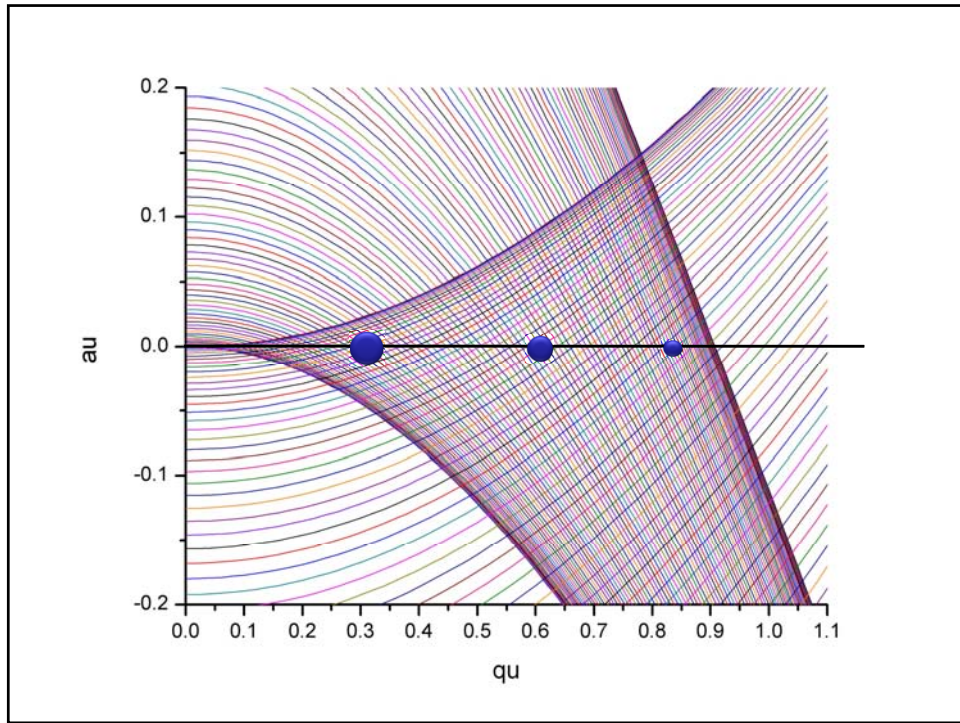
$$a_z = -2a_r = \frac{-16eU}{mr_o^2\Omega^2}$$

$$q_z = -2q_r = \frac{-8eV}{mr_o^2\Omega^2}$$

$R \propto t_{trap} \approx \# RFcycles$





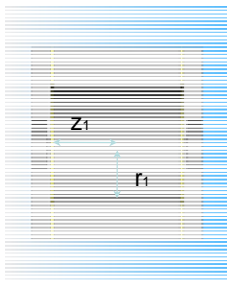


$$a_z = \frac{-16eU}{m(r_0^2 + 2z_0^2)\Omega^2}$$

$$a_z = 0$$

$$q_z = \frac{-8eV}{m(r_0^2 + 2z_0^2)\Omega^2}$$

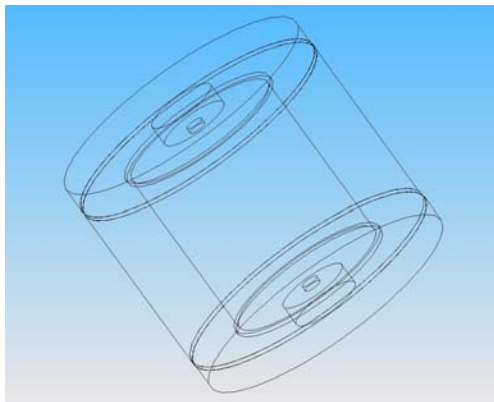
For a cylindrical ion trap, where



$$r_1^2 = 2z_0^2$$

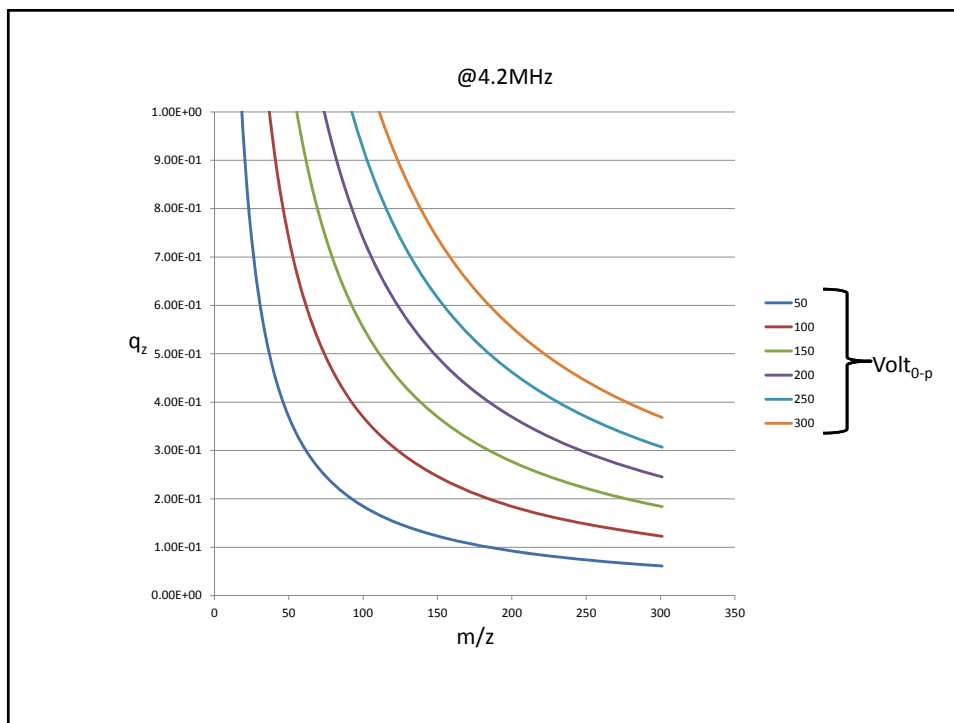
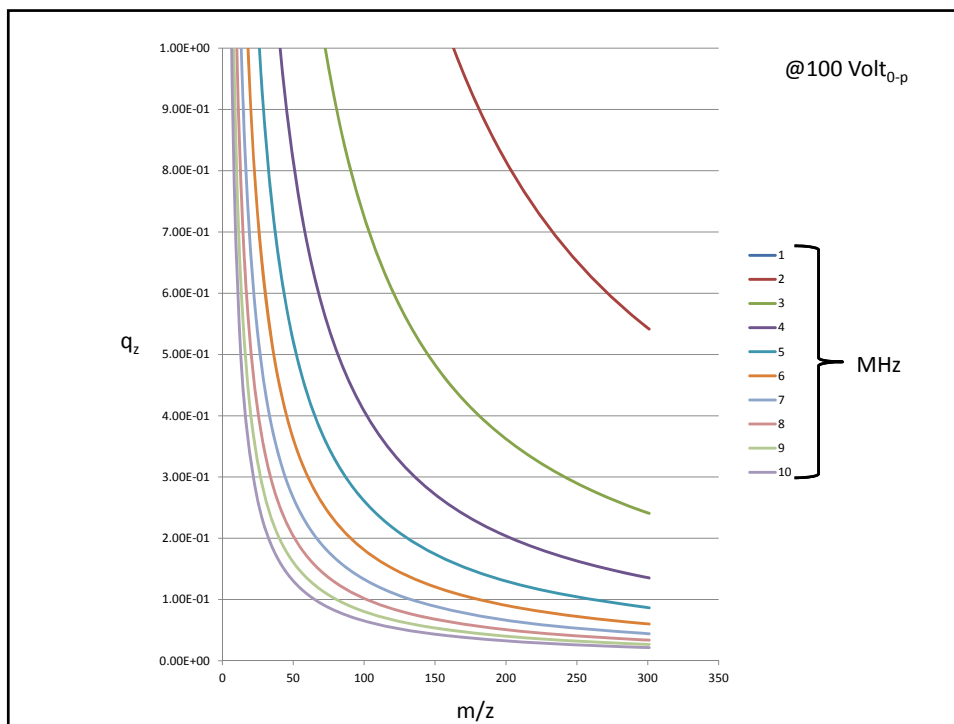
$$a_z = \frac{-8eU}{m(r_1^2)\Omega^2}$$

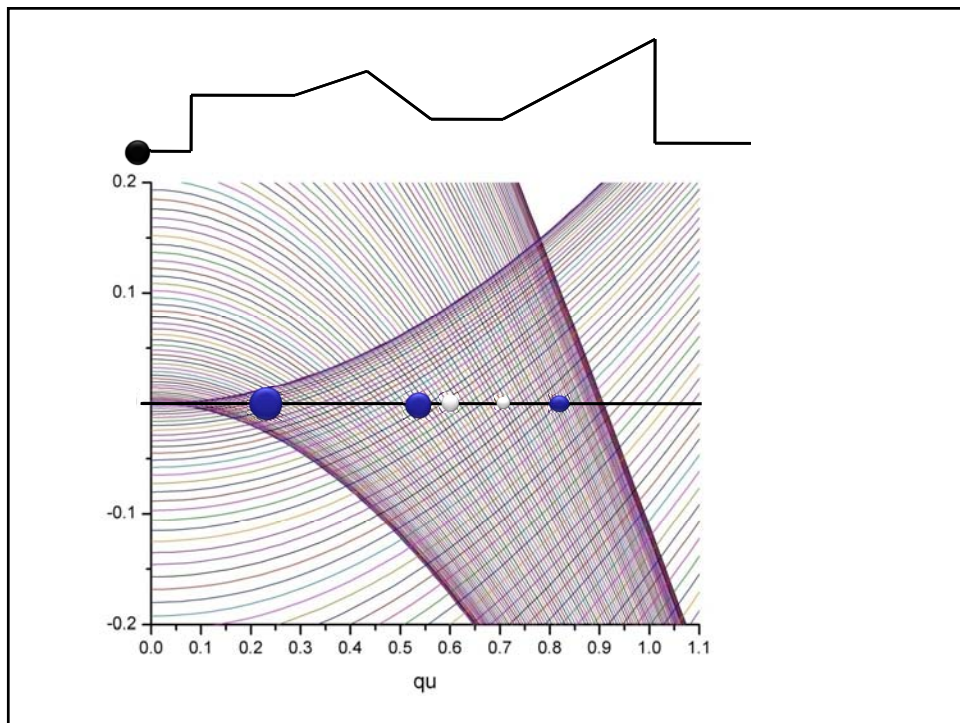
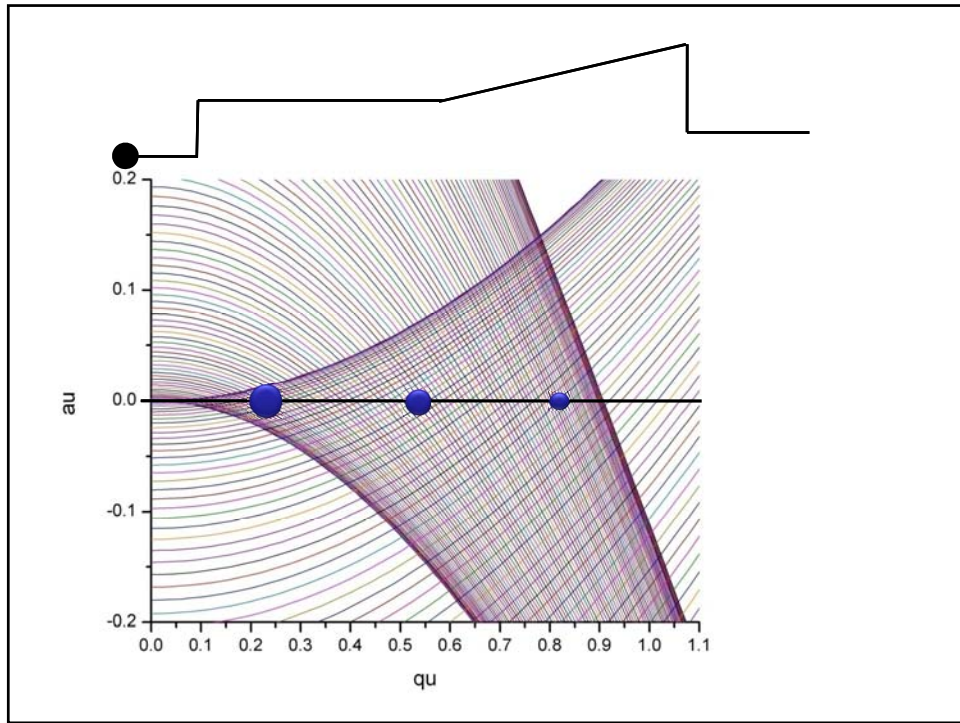
$$q_z = \frac{-4eV}{m(r_1^2)\Omega^2}$$



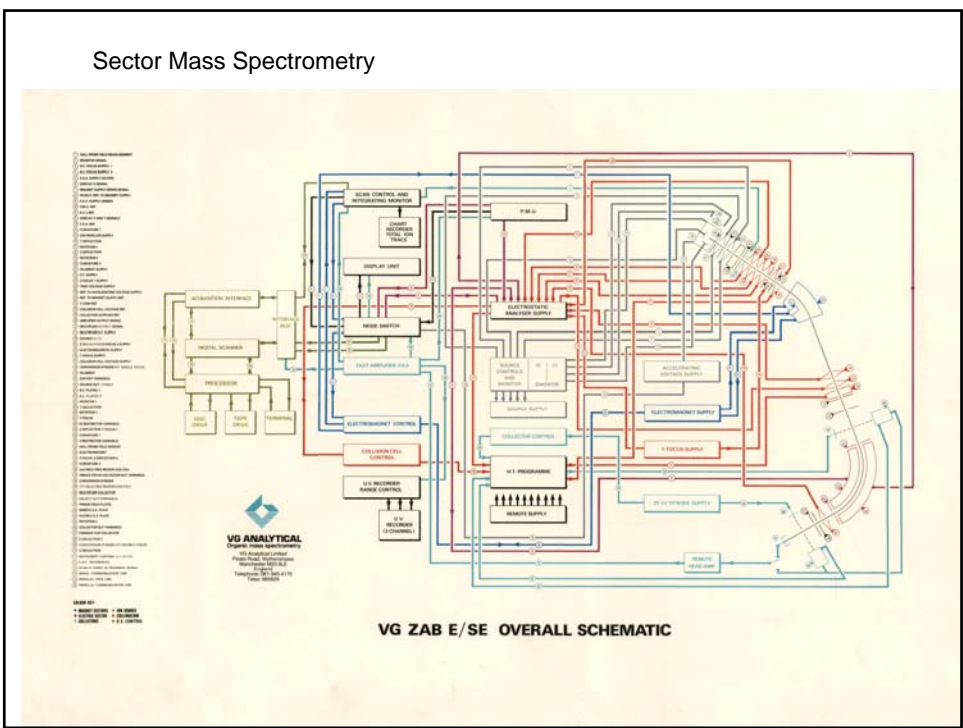
e=	1.60E-19 C									
r=	0.001 m									
Omega=	6000000 Hz					37699112				
m/z	q									
V0-p	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	
10	6.78834807	3.394417	2.262945	1.697209	1.357767	1.131472	0.969834	0.848604	0.754315	
20	13.5776961	6.788835	4.52589	3.394417	2.715534	2.262945	1.939667	1.697209	1.50863	
30	20.3665042	10.18325	6.788835	5.091626	4.073301	3.394417	2.909501	2.545813	2.262945	
40	27.15533923	13.57767	9.05178	6.788835	5.431068	4.52589	3.879334	3.394417	3.01726	
50	33.94417403	16.97209	11.31472	8.486044	6.788835	5.657362	4.849168	4.243022	3.771575	
60	40.73300884	20.3665	13.57767	10.18325	8.146602	6.788835	5.819001	5.091626	4.52589	
70	47.52184365	23.76092	15.84061	11.88046	9.504369	7.920307	6.788835	5.94023	5.280205	
80	54.31067846	27.15534	18.10356	13.57767	10.86214	9.05178	7.758668	6.788835	6.03452	
90	61.09951326	30.54976	20.3665	15.27488	12.2199	10.18325	8.728502	7.637439	6.788835	
100	67.88834807	33.94417	22.62945	16.97209	13.57767	11.31472	9.698335	8.486044	7.54315	
110	74.67718288	37.33859	24.89239	18.6693	14.93544	12.4462	10.66817	9.334648	8.297465	
120	81.46601768	40.73301	27.15534	20.3665	16.2932	13.57767	11.638	10.18325	9.05178	
130	88.25485249	44.12743	29.41828	22.06371	17.65097	14.70914	12.60784	11.03186	9.806095	
140	95.0436873	47.52184	31.68123	23.76092	19.00874	15.84061	13.57767	11.88046	10.56041	
150	101.8325221	50.91626	33.94417	25.45813	20.3665	16.97209	14.5475	12.72907	11.31472	
160	108.6213569	54.31068	36.20712	27.15534	21.72427	18.10356	15.51734	13.57767	12.06904	
170	115.4101917	57.7051	38.47006	28.85255	23.08204	19.23503	16.48717	14.42627	12.82335	
180	122.1990265	61.09951	40.73301	30.54976	24.43981	20.3665	17.457	15.27488	13.57767	
190	128.9878613	64.49393	42.99595	32.24697	25.79757	21.49798	18.42684	16.12348	14.33198	
200	135.7766961	67.88835	45.2589	33.94417	27.15534	22.62945	19.39667	16.97209	15.0863	
210	142.5655309	71.28277	47.52184	35.64138	28.51311	23.76092	20.3665	17.82069	15.84061	
220	149.3543658	74.67718	49.78479	37.33859	29.87087	24.89239	21.33634	18.6693	16.59493	
230	156.1432006	78.0716	52.04773	39.0358	31.22864	26.02387	22.30617	19.5179	17.34924	
240	162.9320354	81.46602	54.31068	40.73301	32.58641	27.15534	23.27601	20.3665	18.10356	
250	169.7208702	84.85044	56.57362	42.43022	33.94417	28.28681	24.24584	21.21511	18.85787	
260	176.509705	88.25485	58.83657	44.12743	35.30194	29.41828	25.21567	22.0371	19.61219	
270	183.2985398	91.64927	61.09951	45.82463	36.65971	30.54976	26.18551	22.91232	20.3665	
280	190.0873746	95.04369	63.36246	47.52184	38.01747	31.68123	27.15534	23.76092	21.12082	
290	196.8762094	98.4381	65.6254	49.21905	39.37524	32.8127	28.12517	24.60953	21.87513	
300	203.6650442	101.8325	67.88835	50.91626	40.73301	33.94417	29.09501	25.45813	22.62945	

For $au=0$,
 $0 < qu < 0.908$





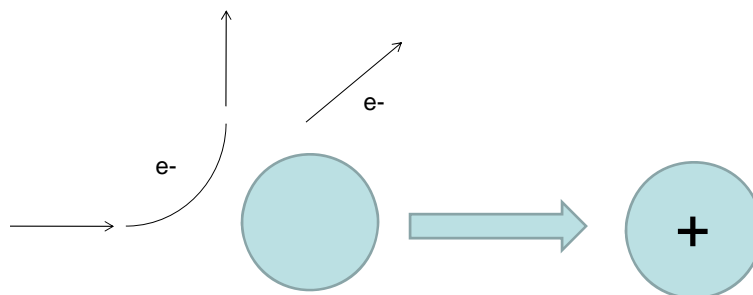
Sector Mass Spectrometry

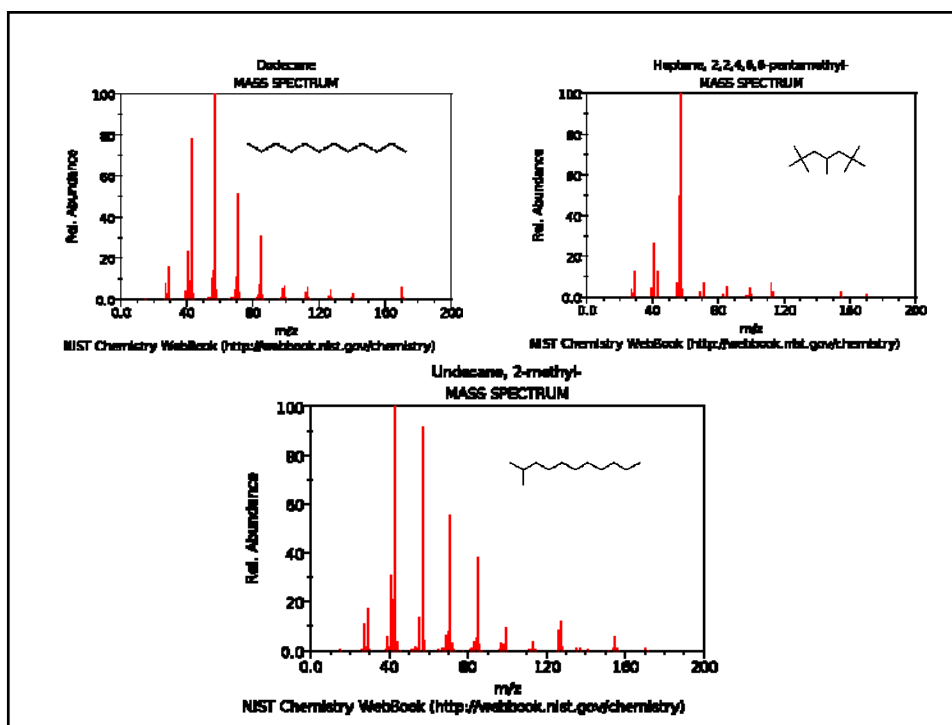
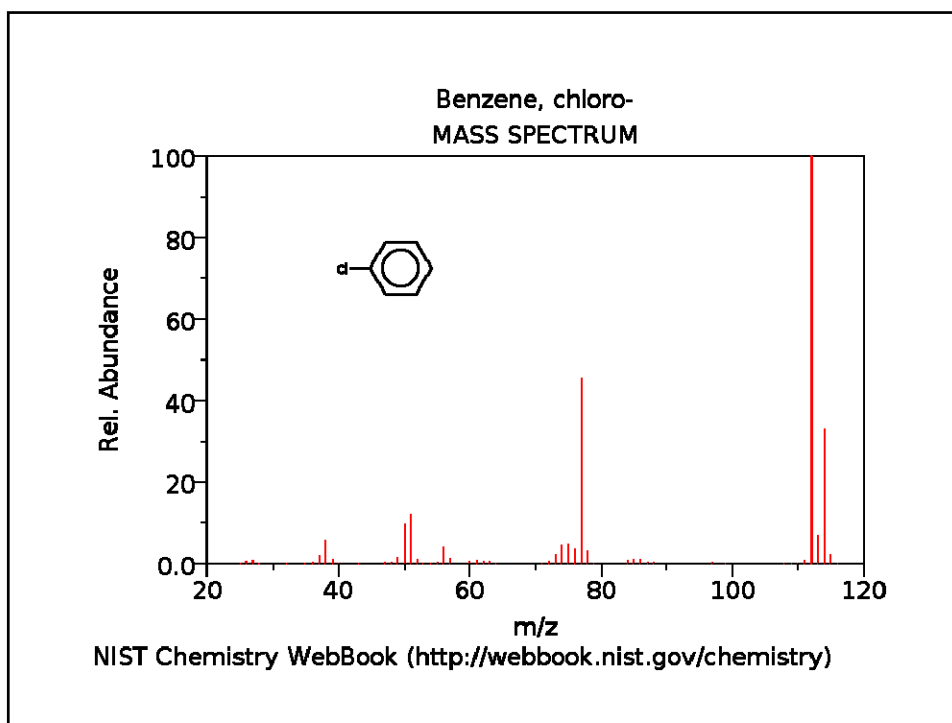


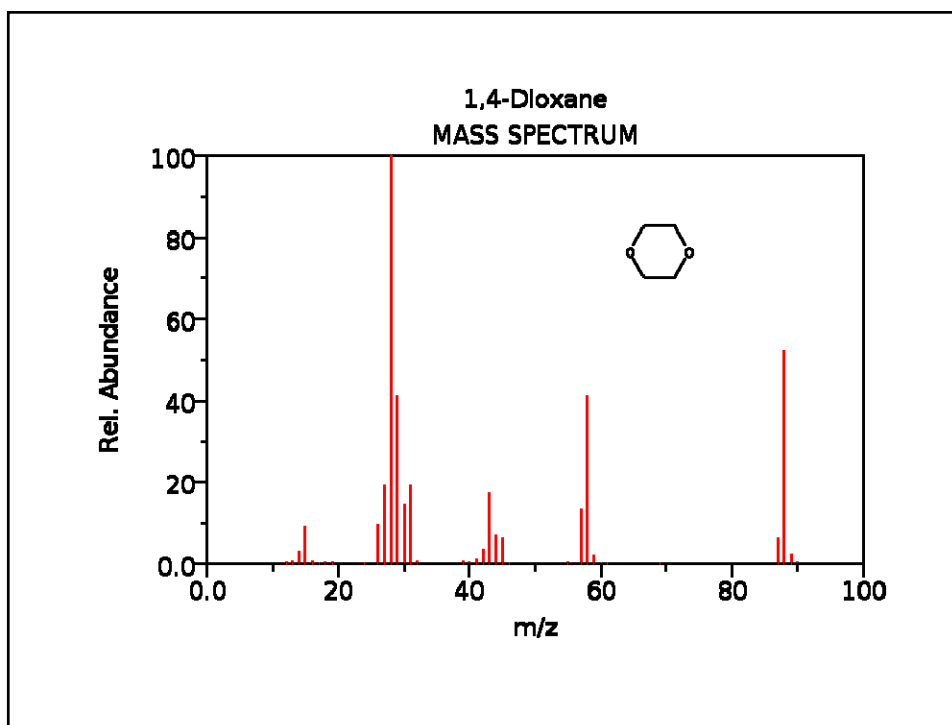
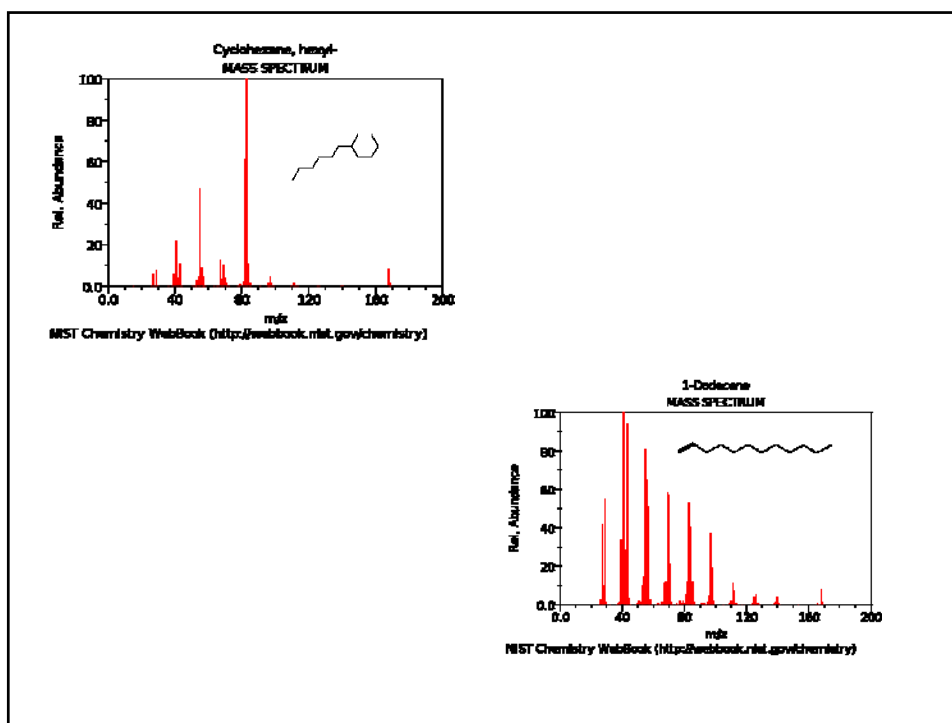
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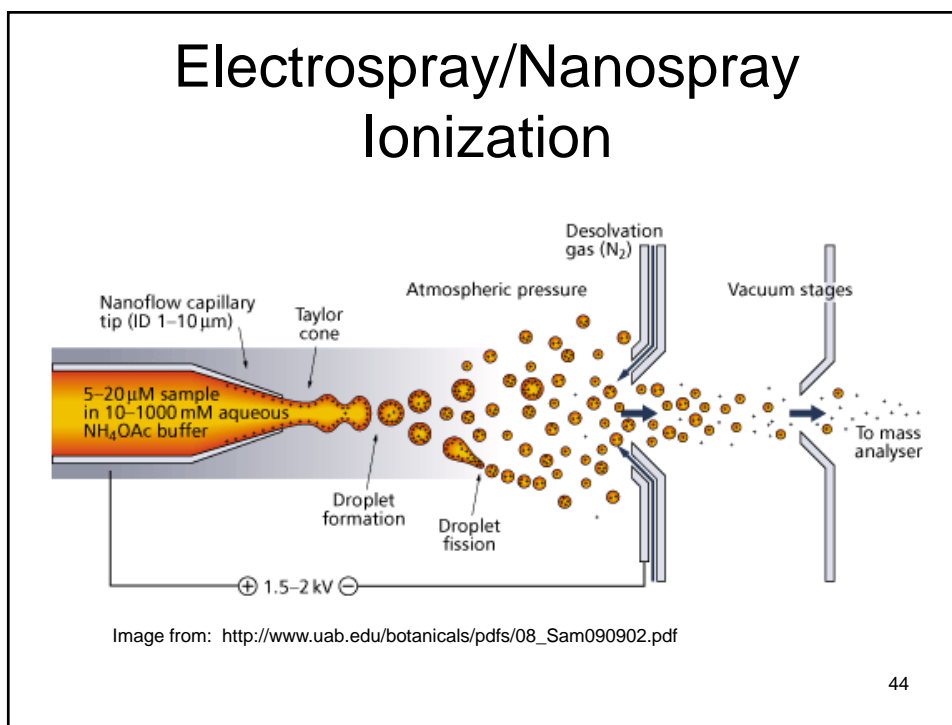
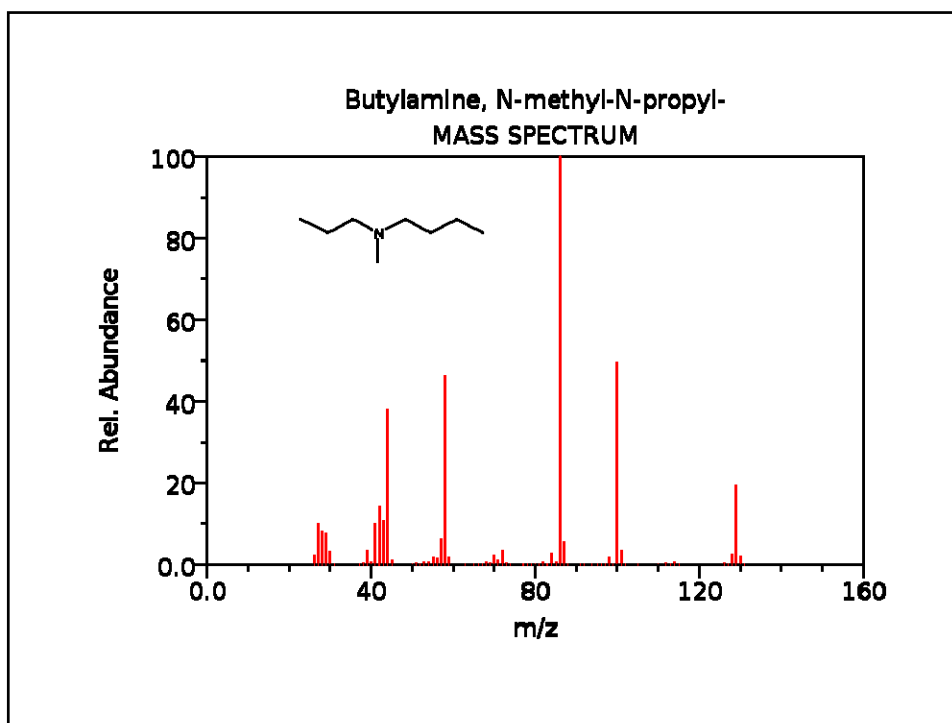


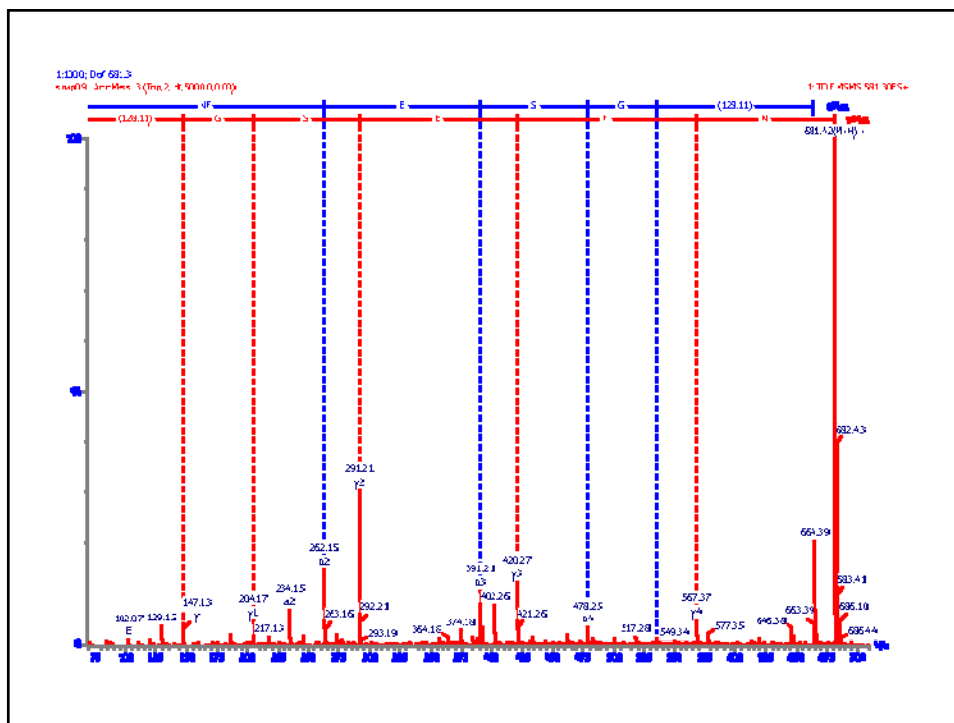
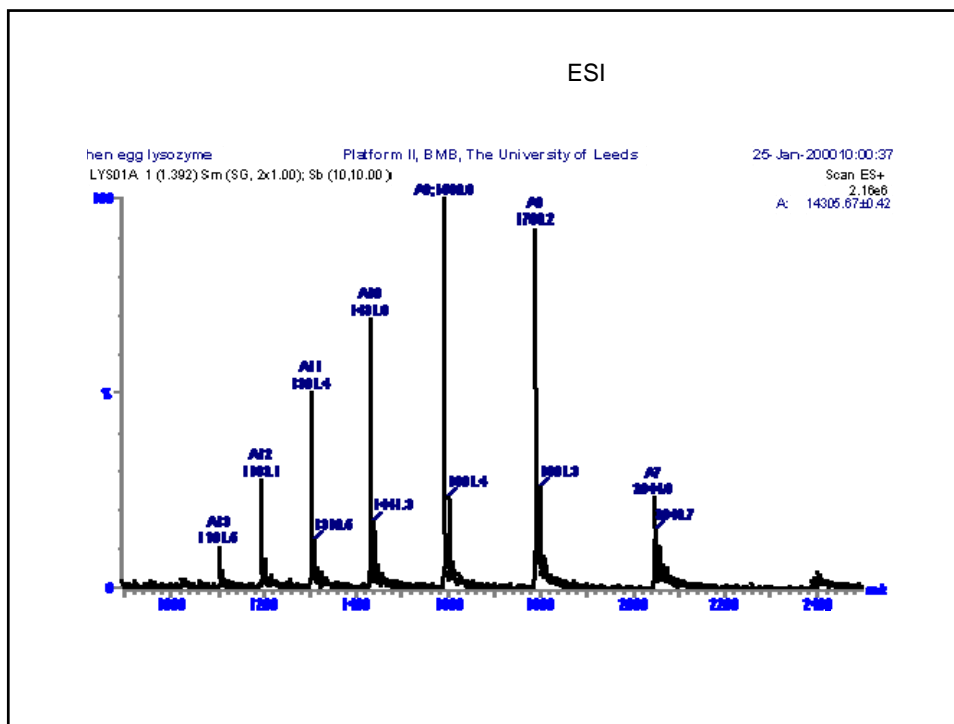
Electron Impact:



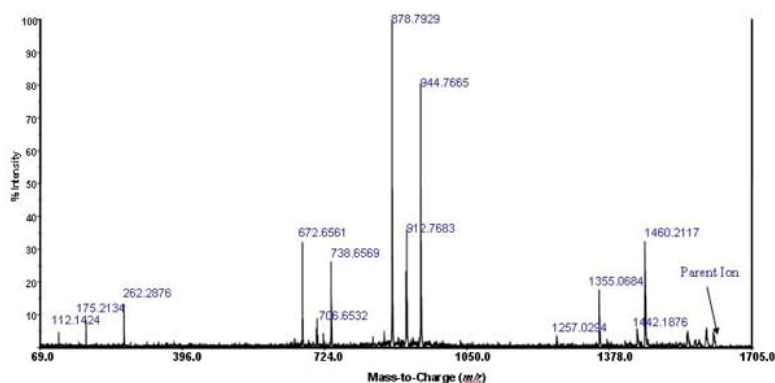




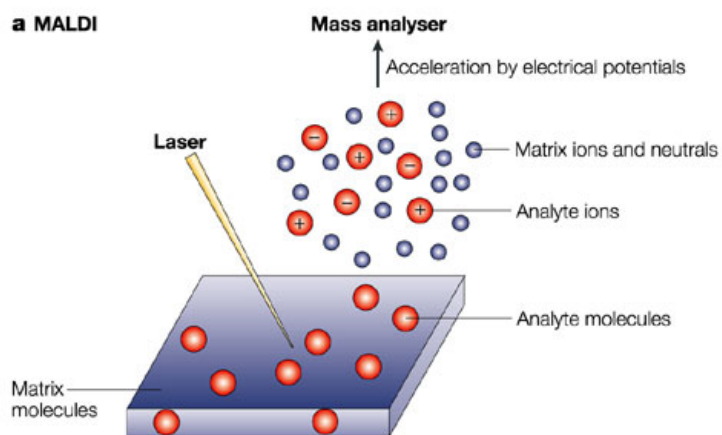




Sample MS/MS Spectrum acquired on the 4700 TOF-TOF of a Digested Protein from Industry



MALDI Ionization



50

Hanno Steen & Matthias Mann *Nature Reviews Molecular Cell Biology* **2004**, 5, 699.

